

# A Data Modem for GSM Voice Channel

Christoph K. LaDue, Vitaliy V. Sapozhnykov, and Kurt S. Fienberg

**Abstract**—This paper introduces a novel approach to data communication over the Global System for Mobile Communications (GSM) voice channel. It is based on the concept of “symbols”—a set of predefined signals with finite bandwidths. Data are encoded into the symbols, and the symbols are voice coded as they were speech, modulated into the GSM signal, sent over the air, GSM demodulated, voice decoded, and converted back to data. The symbols are synthesized by a genetic algorithm with the aim of maintaining separability after passing them through the voice codec. This method enables data transfer over communication networks that do not have dedicated data channels and could also be used in conjunction with other data services to balance the system load between data and voice channels, allowing optimization of system resources. We present the full algorithmic structure of the system, which performs data communications over the GSM voice channel, and we also give the results of the performance tests.

**Index Terms**—Data communications, genetic algorithms (GAs), mobile communications, vocoders.

## I. INTRODUCTION

WIRELESS communication has already become a part of our daily lives, and it continues to rapidly expand and evolve, covering greater area and offering broader services. There exists a plethora of different communication network architectures and methodologies such as CDMA, CDMA2000, Universal Mobile Telecommunications System, Global System for Mobile Communications (GSM), etc.. Whereas the majority of the development effort is concentrated on new technologies, older preexisting networks have some practical advantages such as low cost, wide coverage, reliability, and acceptance by many local authorities. Among them, the GSM network is probably the most ubiquitous and internationally accepted. Thus, it would be advantageous to add new and improved functionality to the legacy networks.

One of the most sought-after improvements is to add data transmission ability to originally “voice-only” networks such as GSM. The most common data channel added to the GSM network is the General Packet Radio Service (GPRS) [1]. The GPRS data traffic, which is also known as the 2.5 generation wireless, and the GSM voice traffic share the same radio channel [2]. To avoid damage to the quality of service (QoS) for GSM voice traffic, voice is given priority, and only the residual capacity of the network is left for GPRS. Therefore, GPRS

available resources are dependent on the voice traffic load, which dominates the GSM network and has an unpredictable (random) nature [2], [3]. This means that queuing delay and outage probability grow with increasing voice traffic, leading to poor QoS for GPRS [3], [5], [8]. Many existing GSM networks have only limited capacity for GPRS, and operators usually need to invest in extending it [4], which is quite costly and may not always be economically feasible. The capacity for data transfer can be significantly increased by moving to the enhanced GPRS, which involves the upgrading of the GSM network with Enhanced Data for Global Evolution (EDGE) technology [9]. However, not only does this require further investment, but QoS issues still remain under conditions of very high traffic load [10]. In addition, GPRS has noncontinuous coverage and interoperability issues [2], [6].

These factors can significantly hinder the use of the GSM data channel. A solution to some of these problems would be to use the compressed speech channel itself to transfer data under some conditions and for some select applications. This technology would obviously be of use in those areas where there is a GSM network but no data service coverage, which is most common in rural areas and developing nations. However, in the likely case that there is already GPRS service available, data transmission through the voice channel would still be useful. Under high-load conditions, when there is a significant probability of outage as the GPRS packet is blocked by voice calls, transferring data through the compressed speech channel would provide better QoS for the data transmission (as the voice traffic has higher priority than the data traffic). This would effectively create a subset of data traffic with higher priority, particularly useful for short data transmissions for which it is important that each data packet be transferred as soon as possible. This could be implemented by carriers who may wish to charge more for higher priority data or by operators who wish higher priority on their data streams independent of the carriers (because the system presented here is a simple voice call as far as the carrier is concerned). In addition, in low-load conditions where there is little voice traffic, a system of data transfer through the compressed voice channel could allow carriers to balance the system load between slots allocated to data and those designated as voice only. Hence, if used along with GPRS, data transmission through the compressed voice channel would allow the balance of the network traffic, maintaining the same QoS for both data and voice.

It should be clear that the modem presented here is not envisaged as a global replacement or direct competition for GPRS or other data transmission systems but as a complementary system to be used for certain applications and situations. In general, communicating data over the voice channel is particularly appropriate for mobile low-bit-rate applications

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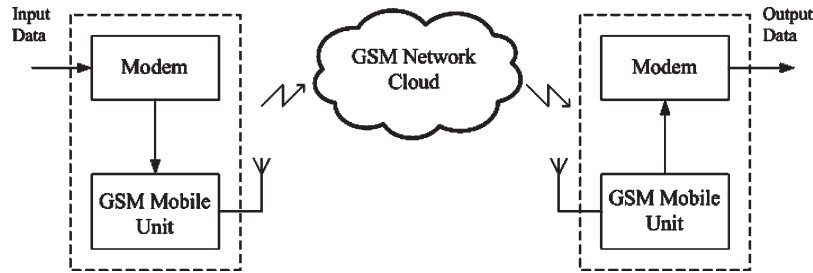


Fig. 1. General system outline.

95 due to potentially higher QoS (due to higher priority), quicker  
 96 connection times, and more ubiquitous coverage compared to  
 97 the dedicated data channels. The last of these, i.e., the wider  
 98 coverage of GSM voice channel, is particularly important for  
 99 vehicular applications in which the modem is expected to move  
 100 to a wide range of locations.

101 The problem in developing such a system lies in the fact  
 102 that GSM voice channel is effectively a band-limited nonlinear  
 103 channel with memory, which is designed for voice-like signals.  
 104 To allow greater channel capacity, the GSM voice codec ex-  
 105 tracts the parameters characterizing speech according to the  
 106 corresponding speech model, and only these parameters are  
 107 sent over the air [7], [11], [12]. At the receiver side, these  
 108 parameters are used to generate a replica of the original speech.  
 109 The compression rate depends on the type of voice codec and  
 110 varies between 8 and 21.9 [7], [12]. Although to the human ear  
 111 the regenerated speech sounds very similar to the original, its  
 112 waveform can in fact be quite different. Hence, it is problematic  
 113 to achieve reasonable error rates while communicating data  
 114 over the compressed voice channel because data communica-  
 115 tion relies on sample-by-sample matching and not on perceptual  
 116 similarity. An obvious way to compensate for the voice coding  
 117 impact is to apply equalization [13], [14]. However, this would  
 118 require the (direct or indirect) identification of the voice codec  
 119 inverse. The nonlinear nature and differential encoding of the  
 120 speech parameters make this voice channel practically uniden-  
 121 tifiable in terms of structures usually used as equalizers, e.g.,  
 122 finite and infinite impulse response, decision feedback, lattice,  
 123 etc. [13], [15].

124 Data communication over the GSM voice channel has a  
 125 unique set of problems that stipulate a conceptually new ap-  
 126 proach specifically targeted to the task. The goal of this paper  
 127 is to design a modem capable of communicating data through  
 128 such a compressed speech medium. This modem is an addition  
 129 to the existing GSM system. (Fig. 1).

130 It converts input data to a pulse-code modulation stream,  
 131 which is fed into a GSM mobile unit exactly as if it were speech.  
 132 The GSM mobile unit encodes and modulates this signal as  
 133 per GSM standard [16] and sends it over the air. The receiver  
 134 GSM unit demodulates and decodes the received signal, which  
 135 is, in turn, fed into the modem. The modem outputs estimates of  
 136 the sent data. Thus, the proposed modem is represented by an  
 137 encoder/decoder pair that encodes raw data into a signal, which  
 138 is treated by the GSM system as speech, lets a GSM mobile unit  
 139 accomplish over-the-air transmission, and decodes this signal  
 140 back into data. As far as the GSM network is concerned, it is a  
 141 normal voice call.

There are two design constraints on the signal.

142

- 1) It has to pass through the voice channel without raising  
 any alarms (e.g., voice activity detector [7]) and fit into  
 the voice band to avoid distortions caused by filtering.
- 2) It has to be robust against the GSM voice coder. “Robust-  
 ness” implies that the signal can be successfully decoded  
 after having been passed through the GSM voice codec.

The general approach to generate a signal, which meets the  
 given constraints, is to apply evolutionary optimization. A ge-  
 netic algorithm (GA) is used to build the desired signal as a set  
 of waveforms (symbol dictionary). This process is accom-  
 plished offline as a modem design procedure. The modem takes  
 these pregenerated symbols and maps the input data onto them.  
 The symbols are concatenated and sent over the air via the GSM  
 unit. On the receiver side, the symbol outputs of the GSM  
 are converted back to data. The data estimate is the index of the  
 symbol from the codebook that maximizes the inner product  
 with the received symbol [this method is further referred to as  
 the maximum dot product (MDP) method]. The actual over-the-  
 air transmission is handled by the existing GSM system with  
 its own modulation, forward error correction (FEC), forward  
 error detection (FED), and equalization. Thus, if their correct  
 functioning is assumed, the major source of errors is the voice  
 codec itself.

One approach to utilize the GSM voice channel for secure  
 voice and/or data communications has already been presented  
 in [17]. Katugampala *et al.* described a system where encrypted  
 voice was modulated into a signal using a speech model so  
 that the waveforms possess speech characteristics to minimize  
 distortions caused by speech compression and to avoid voice  
 activity detection (VAD) [18]. These waveforms were then  
 transmitted over the GSM voice channel and demodulated and  
 decrypted at the receiver.

The fundamental difference between the method described  
 in [17] and the method presented in this treatment lies in the  
 way the data are mapped onto the waveform and extracted  
 from it. In [17], these waveforms are speech-like as they are  
 generated using a particular speech model [18]. Thus, at the  
 transmitter, the digital data were “hard coded” into a set of  
 speech-specific parameters according to the speech model and  
 extracted from the waveforms by a speech parameter estimator  
 at the receiver. Therefore, the effects of voice transcoding and  
 VAD were minimized by using a “speech-like” signal. Con-  
 versely, in the data transmission method described in this paper,  
 the waveforms used to transmit the data do not necessarily  
 possess speech characteristics or fit any preassumed model.

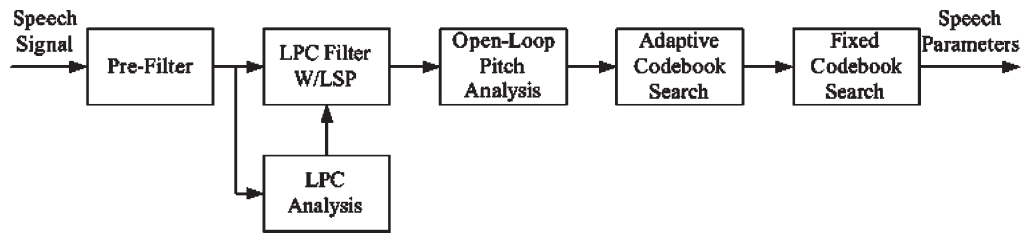


Fig. 2. Generalized ACELP voice-encoding process.

188 They are generated by the GA to be robust to the voice coding.  
 189 Distortions caused by the voice-coding/decoding processes are  
 190 alleviated by maximizing the Euclidian distances between the  
 191 band-limited waveforms after transmission, and the VAD is  
 192 avoided by dynamically varying their spectral envelopes. As  
 193 it will be seen, this leads to a much simpler design, which  
 194 can easily fit into an embedded system and allows higher  
 195 data rates.

196 This paper is organized as follows. Section II presents the  
 197 theoretical basis of the GSM voice channel. Section III outlines  
 198 the general modem description, including data-to-symbol en-  
 199 coding and symbol-to-data decoding procedures. Section IV de-  
 200 scribes the evolutionary symbol-generation process. Sections V  
 201 and VI present an example implementation and numerical  
 202 simulations. Section VII discusses the results and considers  
 203 further implications.

## 204 II. GSM VOICE CODEC

205 The GSM standard [16] currently supports the following four  
 206 speech compression techniques: 1) full rate; 2) enhanced full  
 207 rate (EFR); 3) adaptive multirate; and 4) half rate. The voice  
 208 codecs, or vocoders, are designed to compress speech signal at  
 209 the transmitter and accurately regenerate it at the receiver.

210 The digitized speech signal with a resolution of 13 b and a  
 211 sampling rate of 8 kHz forms the input to all the GSM speech  
 212 codecs. The encoder extracts the speech parameters, which are  
 213 then arranged into a bitstream. The output rate of the speech en-  
 214 coder depends on its type [12]. The parameterized compressed  
 215 speech signal is encoded and modulated according to the GSM  
 216 specification and sent over the air. After demodulation, the  
 217 bits are fed into the speech decoder to synthesize the original  
 218 speech. In this paper, we consider the GSM EFRV voice codec  
 219 (EFRV). However, the approach should be general enough to  
 220 be applied to other voice codecs, as will be further discussed in  
 221 Section VII.

222 The EFRV is a lossy voice codec that performs mapping  
 223 between input speech bursts to encoded bit blocks and from  
 224 encoded bit blocks to reconstructed speech samples, yielding a  
 225 compression ratio of 8.5 times and a bit rate of 12.2 kb/s for the  
 226 encoded bitstream. The coding scheme used for compression/  
 227 decompression is the algebraic code-excited linear prediction  
 228 (ACELP) coder [19]. The EFRV uses a 10th-order short-term  
 229 linear prediction and a long-term linear prediction filters. These  
 230 filters are excited with a combination of adaptive and algebraic  
 231 codebooks (sets of excitation vectors). The general form of the  
 232 encoding process is illustrated in Fig. 2 and can be described as  
 233 follows.

After prefiltering and downscaling, the short-term analysis is  
 performed twice per frame (each 20-ms voice frame comprises  
 four equal subframes). It consists of autocorrelation with two  
 asymmetric windows of 30 ms each, concentrated around every  
 second subframe. The results are converted to short-term lattice  
 filter coefficients and then to line spectral pairs. An open-  
 loop pitch analysis is then performed twice per frame to find  
 two initial estimates of the pitch lag (delay) for each frame.  
 These delays and a grid of delays around them are fed into  
 the speech synthesizer, and its output is compared against the  
 nonsynthesized input. The pitch lags and the gains that corre-  
 spond to the minimum weighted error are chosen and quantized.  
 The residual signal remaining after the quantization of the  
 adaptive codebook search is modeled by the algebraic codebook  
 using the same approach—synthesize all the possibilities, and  
 choose the one that corresponds to the minimum error. All the  
 calculated speech parameters are packed into the coded speech  
 frame and sent into the GSM physical layer for transmission.  
 The decoding process is represented in Fig. 3.

The parameters of the decoder are set by the values from  
 the received coded speech frame. The speech samples are  
 synthesized by exciting the linear prediction filter with the sum  
 of the algebraic and adaptive codebooks. Although, to a human  
 listener, the reconstructed speech may sound very similar to the  
 original, the waveform is often very different when comparing  
 sample by sample. The vocoder is based on linear prediction  
 and differential encoding of the speech parameters, both of  
 which assume correlation between samples. This assumption  
 holds for voice, which is relatively smooth and slowly changes  
 over time. On the other hand, this is not generally the case  
 for conventional data signals. The more data are transmitted  
 within a fixed bandwidth, the less correlated the samples are.  
 This, in turn, means that the signal fits less into the speech  
 model causing greater distortions and higher error rates. It  
 makes data transmission through the GSM-compressed voice  
 channel a challenge that requires new techniques. As described  
 in Section I, one such technique was presented in [17], but it is  
 quite different compared to our approach, and a comparison of  
 the results is presented in Section VI.

Because of the vocoder's nonlinear nature and memory, it  
 is virtually impossible to represent it by an analytic transfer  
 function. Indeed, the speech-coding process involves multiple  
 quantizations with differential encoding, which causes loss of  
 information about the original signal. The feedback and mem-  
 ory then magnify and propagate these distortions. Moreover, the  
 vocoder output depends not only on the input signal but on its  
 own state as well, which in turn is defined by the previous signal  
 frames including errors. Thus, the concept of conventional

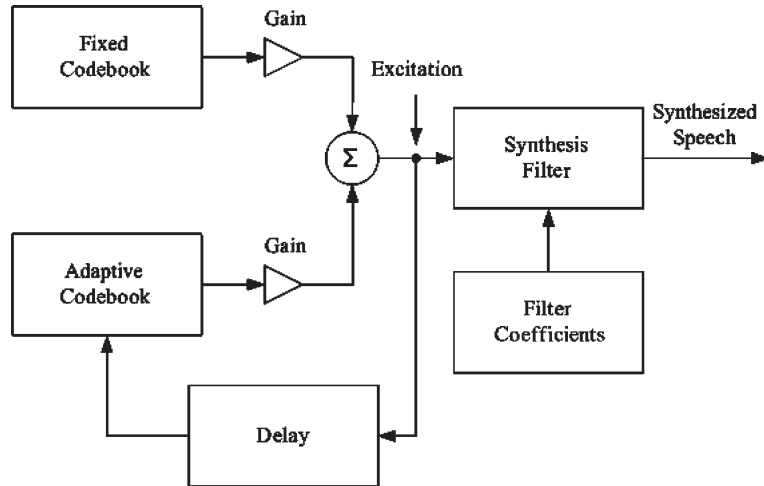


Fig. 3. Generalized ACELP voice-decoding process.

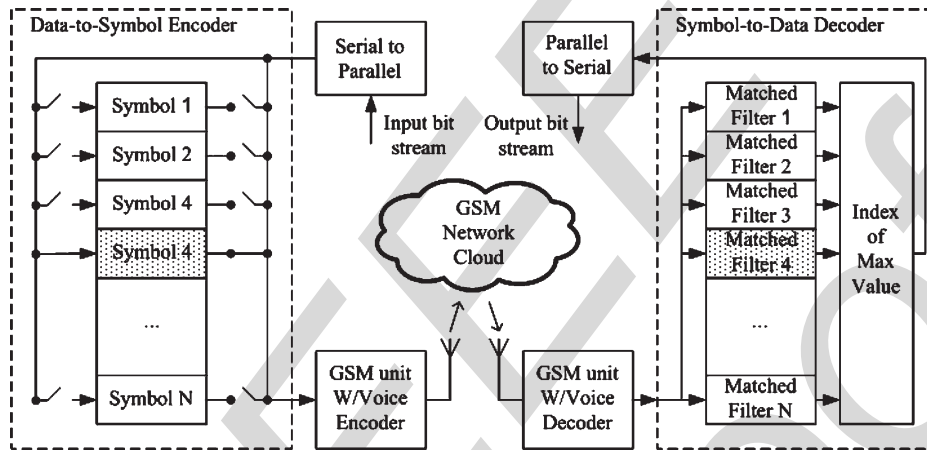


Fig. 4. General modem structure. The “data-to-symbol” encoder is a table lookup that maps the decimal data words onto the symbols. The “symbol-to-data” decoder estimates the sent data words using the MDP method.

282 equalization (or the “inverse vocoder”) is not applicable  
283 in this case.

### 284 III. GENERAL MODEM DESCRIPTION

285 One possible way to enable data transfer through the GSM  
286 voice codec is to design a set of waveforms, which are symbols  
287 that fit into the voice band (300–3400 Hz) and that can be  
288 successfully decoded after passing them through the vocoder.  
289 The data are mapped onto these symbols on the transmitter  
290 side and extracted from them on the receiver side. Thus, this  
291 method represents a “data precoding” technique that is followed  
292 by the conventional GSM system. In this section, we describe  
293 “data-to-symbol” encoding and “symbol-to-data” decoding. A  
294 method to generate the symbols will be detailed in Section IV.  
295 The general structure of our modem is shown in Fig. 4.

296 The “data-to-symbol” encoding consists of the follow-  
297 ing steps.

- 298 1) Divide the incoming data bitstream into decimal words  $i$   
299 of  $N_{\text{bit}}$  bits each.
- 300 2) Using these words, address the dictionary  $\mathbf{D}$ , which is  
301 the table containing the symbols  $\mathbf{s}_i$ ,  $i = 1, 2, \dots, N_{\text{sym}}$ ,

where  $N_{\text{sym}} = 2^{N_{\text{bit}}}$  is the number of symbols in the 302  
dictionary. Thus, a single decimal scalar  $i$  is encoded 303  
into a single vector symbol  $\mathbf{s}_i$  by a mapping  $M$  304  
given by 305

$$M : \mathbf{I} \rightarrow \mathbf{D} \quad (1)$$

where 306

$$\begin{aligned} \mathbf{I} &= \{1, 2, \dots, N_{\text{sym}}\} \\ \mathbf{D} &= \{\mathbf{s}_1, \mathbf{s}_2, \mathbf{s}_3, \dots, \mathbf{s}_{N_{\text{sym}}}\}. \end{aligned} \quad (2)$$

These symbols are scaled to 13-b integers, concatenated, and 307  
framed into packets. The packets are then fed into the GSM 308  
unit as though they formed an audio signal. In the GSM unit, 309  
they are passed through the voice encoder, modulated according 310  
to the GSM standard, and sent over the air. On the receiver 311  
side, the incoming signal is demodulated and passed through 312  
the voice decoder. Then, the GSM unit output is fed into the 313  
“symbol-to-data” decoder, which

- 314 1) deframes symbol packets and determines the beginning 315  
of the first symbol; 316

317 2) gets each received symbol and decides which symbol  
318 is most likely to have been transmitted. Its index in  
319 the dictionary represents the estimate of the transmitted  
320 decimal word  $\hat{i}$ , which in turn is converted to the output  
321 data bitstream.

322 As mentioned above, it is impossible to express the GSM  
323 EFRV in terms of transfer function in closed form. On the  
324 other hand, the voice-encoding/decoding processes can be rep-  
325 resented as an operator given by

$$\mathbf{y} = \mathbf{y}(s_i, \psi) = V(s_i, \psi) \quad (3)$$

326 where  $\mathbf{y}$  is the symbol  $s_i$  after the voice-encoding/decoding  
327 processes,  $\psi = \Psi(\{s_k\}_{k=1}^{i-1}, \psi_0)$  is the voice codec state, which  
328 depends on all previous inputs since the vocoder was re-  
329 set to its initial state  $\psi_0$ , and  $V(\cdot)$  represents the vocoder-  
330 encoding/decoding processes.

331 It is convenient to formulate the problem on hand in terms of  
332 classical signal detection theory [20]. The transmitter sends dig-  
333 ital data encoded into a set of symbols  $\{s_i, i = 1, \dots, N_{\text{sym}}\}$   
334 through the GSM EFRV. The receiver observes the signal  $\mathbf{y}$  and  
335 tries to decide which  $s_i$  out of  $N_{\text{sym}}$  symbols was most likely  
336 sent. Thus, the symbol-to-data-detection process can be viewed  
337 as the *a posteriori* probability distribution maximization

$$\hat{i} = \arg \max_i [P(s_i | \mathbf{y})] \quad (4)$$

338 where  $P(s_i | \mathbf{y})$  is the probability distribution of the sent sym-  
339 bols  $s_i$  given the received symbol  $\mathbf{y}$ . Because the vocoder  
340 output depends not only on the sent symbol but also on its state,  
341 the received symbols are not independent. This implies that  
342 the *a posteriori* probability distribution should be  $P(s_i | \mathbf{y}, s_1,$   
343  $s_2, \dots, s_{i-1})$ . It is generally possible to model the nonlinear  
344 EFRV as a Markov process to estimate the *a posteriori* distribu-  
345 tion. However, this would lead to an extremely high complexity  
346 of the decision algorithm. To simplify the system design and  
347 implementation, we have ignored the previous  $\{s_k\}_{k=1}^{i-2}$  sym-  
348 bols at the cost of some error performance degradation. The  
349 decision to truncate the history here is based on the fact that the  
350 complexity would exponentially increase with each symbol of  
351 the historical series included in the decoding process (combined  
352 with the desire to implement the modem in a cheap portable  
353 device). In addition, there is a relatively small gain in decoding  
354 performance for each additional symbol included. Although  
355 there is a dependence on history in the vocoder, the method  
356 of the differential coding used means that this dependence has  
357 a “long memory” and would have to include the entire history  
358 since the last reset to provide significant decoding performance.  
359 Hence, we use only  $P(s_i | \mathbf{y})$  for the *a posteriori* probability.  
360 Bayes’ rule gives the *a posteriori* probability dis-  
361 tribution [20]

$$P(s_i | \mathbf{y}) = \frac{P(s_i)P(\mathbf{y} | s_i)}{P(\mathbf{y})} \quad (5)$$

362 where  $P(s_i)$  is the *a priori* probability distribution of  $s_i$ ,  
363  $P(\mathbf{y} | s_i)$  is the likelihood function of  $\mathbf{y}$ , and  $P(\mathbf{y})$  is the *a priori*

probability distribution of  $\mathbf{y}$ . It should be noted that the likeli- 364  
hood function  $P(\mathbf{y} | s_i)$  also does not include previous symbols 365  
 $\{s_k\}_{k=1}^{i-2}$  to avoid excessive decoding algorithm complexity. 366  
The probability  $P(\mathbf{y})$  is independent of the transmitted symbol 367  
 $s_i$ , so if  $P(s_i)$  is assumed to be uniformly distributed (e.g., 368  
can be forced by scrambling), then the symbol detection can 369  
be reduced to the maximum likelihood estimation 370

$$\hat{i} = \arg \max_i [P(\mathbf{y} | s_i)]. \quad (6)$$

To proceed, some knowledge of the likelihood function is re- 371  
quired. Simulation experiments were used to estimate statistical 372  
properties of  $P(\mathbf{y} | s_i)$  by encoding random data into symbols 373  
and then passing them through the voice codec and observing 374  
the distribution of the received symbols. We discovered that 375  
 $P(\mathbf{y} | s_i)$  was ergodic, bell-shaped, and of finite variance. In 376  
addition, it was noted that  $P(\mathbf{y} | s_i)$  was not necessarily centered 377  
on  $s_i$ . However, the MDP estimation does not require the distri- 378  
bution to be inherently centered. It can always be accomplished 379  
by subtracting the mean value  $\bar{\mathbf{y}}(s_i)$  given by 380

$$\bar{\mathbf{y}}(s_i) = E[\mathbf{y}(s_i, \psi)] \quad (7)$$

where  $E[\cdot]$  represents expected value over all the voice codec 381  
states  $\psi$ . 382

The process of estimating  $\bar{\mathbf{y}}(s_i)$  involves encoding a sta- 383  
tistically sufficient amount of random data into the symbols, 384  
performing the voice-encoding/decoding processes, and calcu- 385  
lating the ensemble average on a symbol-by-symbol basis. The 386  
mean symbol  $\bar{\mathbf{y}}(s_i)$  can be calculated offline because the GSM 387  
EFRV is standardized and available in software [21]. Hence, it 388  
is possible to factorize (3) by 389

$$\mathbf{y} = \bar{\mathbf{y}}(s_i) + \mathbf{n}(s_i, \psi) \quad (8)$$

where  $\mathbf{n}(s_i, \psi)$  is the irregular part of the received signal 390  
that depends on both the current vocoder state and the input 391  
symbol. This can be thought of as an “effective noise” caused 392  
by the voice-encoding/decoding processes. Due to the fact 393  
that  $\mathbf{n}(s_i, \psi)$  depends on the sent symbol  $s_i$ , the effective 394  
signal-to-noise ratio also depends on  $s_i$  and, therefore, cannot 395  
be improved by simply increasing signal power. With these 396  
properties, after the removal of the mean value, the likelihood 397  
function  $P(\mathbf{y} | s_i)$  can be approximated as a centered Gaussian 398  
process, with its variance dependent on  $s_i$  as given by 399

$$P(\mathbf{y} | s_i) = \frac{1}{\sqrt{2\pi\sigma_i^2}} \exp\left\{-\frac{\|\mathbf{y}(s_i, \psi) - \bar{\mathbf{y}}(s_i)\|^2}{2\sigma_i^2}\right\} \quad (9)$$

where  $\|\cdot\|$  denotes Euclidean distance, and  $\sigma_i^2$  is the “effective” 400  
noise variance for the symbol  $s_i$ . 401

Substituting (9) into (6) and simplifying the result gives 402

$$\hat{i} = \arg \min_i \left[ \|\mathbf{y}(s_i, \psi) - \bar{\mathbf{y}}(s_i)\|^2 \right]. \quad (10)$$

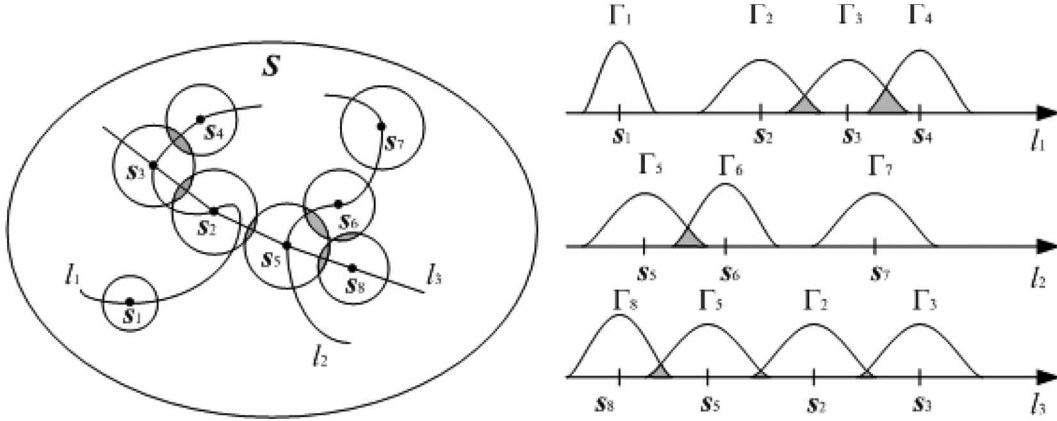


Fig. 5. Symbol space. Points  $s_i$  illustrate the transmitted symbols in the symbol space  $S$ . The circles around them show the spread after passing through the vocoder. On the right are the probability distributions  $\Gamma_i$  along the lines  $l_i$ .

403 If all  $s_i$  have equal power (this will be achieved by a design  
404 constraint), then

$$\hat{i} = \arg \max_i \{ \langle \mathbf{y}(s_i, \psi), \bar{\mathbf{y}}(s_i) \rangle \} \quad (11)$$

405 where  $\langle \cdot, \cdot \rangle$  represents vector dot product.

406 Thus, the MDP “symbol-to-data”-decoding process involves  
407 calculating the dot products of the received symbol  $\mathbf{y}(s_i, \psi)$   
408 and all of the precalculated mean symbols  $\bar{\mathbf{y}}(s_i)$ . The index  
409 corresponding to the maximum symbol dot product is the  
410 estimate  $\hat{i}$  of the transmitted data word  $i$ . The MDP detector can

411 be implemented by a bank of matched filters or correlators [20].  
412 Having described the data-to-symbol encoding and symbol-  
413 to-data decoding techniques, we are ready to design the sym-  
414 bols themselves.

#### 415 IV. SYMBOL DESIGN

##### 416 A. Symbol Design as a Search Problem

417 The symbol-generation process can be formulated as a search  
418 problem. The symbols are generated in the frequency domain  
419 so that their frequencies are not allowed to be outside of the  
420 designated bandwidth and their power is normalized. At the  
421 same time, the symbols should be robust enough to still be iden-  
422 tifiable after passing through the voice codec. This robustness  
423 is a relative measure that can be expressed in terms of error  
424 rate. Thus, band limits and unity power form constraints on the  
425 search space, whereas robustness represents a cost function.

426 The search space  $S$  for the optimization problem can be  
427 defined as all discrete symbols of length  $N_{\text{sam}}$  samples in time  
428 whose frequency spectrum  $\Phi$  is contained in the frequency  
429 interval  $[F_{\min}, F_{\max}]$ , i.e.,  $\Phi \in [F_{\min}, F_{\max}]$ . Frequencies  $F_{\min}$   
430 and  $F_{\max}$  should be within the voice band (300–3400 Hz), but  
431 their actual values are dictated by specific carrier requirements.  
432 The search space  $S$  is also constrained by symbol power  $P_{\text{sym}}$ .  
433 The total power of each symbol is normalized.

434 The most obvious cost function  $C(i)$  for the  $i$ th symbol is

$$C(i) = \frac{L_{\text{err}}(i)}{L_{\text{total}}(i)} \quad (12)$$

where  $L_{\text{err}}(i)$  is the number of erroneous detections out of 435  
 $L_{\text{total}}(i)$  times that the  $i$ th symbol was sent over the vocoder. 436  
In practice, the cost function for all symbols is calculated by 437  
encoding a large amount of random data into the symbols, 438  
passing them through the voice codec (including both voice- 439  
encoding/decoding processes), applying MDP symbol-to-data 440  
decoding, and comparing the number of symbol misdetections 441  
with the total number of times that each particular symbol 442  
passed through the voice codec. 443

With the search space and cost function defined, we have a 444  
constrained minimization problem. Due to the discrete nature 445  
of the symbols, the search space is finite dimensional with a 446  
dimension proportional to the number of samples in a symbol 447  
 $N_{\text{sam}}$ . Hence, the search space can potentially have a large 448  
number of dimensions. 449

The cost function is defined by the output of the vocoder 450  
and is difficult to analytically express. However, there are some 451 AQ3  
known features that the cost function possesses. 452

- 1) Nonlinearity comes directly from the vocoder properties. 453
- 2) Cost functions  $C(i)$  for the different symbols will not 454  
be independent because of the MDP decoding (which 455  
implies that the more similar the symbols are, the more 456  
difficult they are to distinguish). In addition, the vocoder 457  
has a memory, thus, the effect on the current symbol 458  
depends on the symbols before it. 459

Fig. 5 illustrates the vocoder impact on the symbols. 460  
The plane  $S$  represents a multidimensional search space 461  
that accommodates symbols  $s_1 = (s_{11}, s_{12}, \dots, s_{1N_{\text{sam}}})$ , 462  
 $s_2 = (s_{21}, s_{22}, \dots, s_{2N_{\text{sam}}})$ ,  $\dots$ ,  $s_8 = (s_{81}, s_{82}, \dots, s_{8N_{\text{sam}}})$  463  
as points. The circles around each point encompass 99% of 464  
all possible vocoder outputs for each corresponding input 465  
symbol. The gray area corresponds to the error probability 466  
 $P_{\text{err}}$  between neighboring symbols. It is more convenient to 467  
visualize the symbol mutual impact along curves  $l_i$ , each of 468  
which goes through the symbols of interest, and  $i = 1, \dots, L$ , 469  
where  $L$  is the number of all possible symbol combinations. 470  
 $\Gamma_i$  denote probabilities of symbol occurrence after passing 471  
the signal through the voice codec. Errors occur where these 472  
probability distributions overlap. Therefore, the greater the 473  
overlap, the higher the cost function  $C(i)$ . It should be noticed 474



475 that an error (misdetection) can potentially happen between  
 476 any symbols from the symbol set. Our goal is to find a symbol  
 477 set from the search space such that probability distributions  
 478 of the symbols—members of this set—have minimal overlap.  
 479 This can be accomplished by cost function minimization.

480 The symbol-generating process is possible to accomplish  
 481 offline because the EFRV is standardized and available in  
 482 software.

### 483 B. GA

484 Synthesizing a set of waveforms (symbol dictionary), which  
 485 satisfies the design specifications mentioned above, is equiva-  
 486 lent to finding a group of points in the signal hyperspace where  
 487 each point represents a symbol. Given that a symbol could  
 488 be a multidimensional vector, the search hyperspace might  
 489 be large and multimodal. Thus, an efficient search algorithm  
 490 is necessary to choose appropriate symbols from the solution  
 491 space. Possible candidates are hill climbing, gradient descent,  
 492 exhaustive search, and simulated annealing [13], [22], [23].  
 493 The gradient descent algorithm is known to be very efficient  
 494 in a unimodal search space when the gradient is available.  
 495 Neither of these two conditions hold in our case. Hill climbing,  
 496 although it does not require explicit gradient information, is not  
 497 suitable for finding global extrema in a multimodal space due  
 498 to its high probability of being trapped in local optima. Thus,  
 499 if the search space is complicated and multimodal, gradient  
 500 descent and hill climbing are not appropriate search algorithms  
 501 for our purpose. Exhaustive search, although not getting stuck  
 502 in the local optima, is not practical in large search spaces. In  
 503 addition, simulated annealing is capable of moving out of local  
 504 minima but heavily depends on the initial conditions. If the  
 505 initial conditions are not properly chosen, it may not be possible  
 506 for simulated annealing to converge to the global optimum.  
 507 Furthermore, simulated annealing requires some smoothness  
 508 of the search space. In the current problem, the search space  
 509 is multidimensional and multimodal, and its exact form is  
 510 unknown and determined by the action of the nonlinear lossy  
 511 GSM voice codec. Thus, the search algorithms described above  
 512 are not the best candidates.

513 A GA is a global optimization technique based on the theory  
 514 of Darwinian evolution and computer science [24], [25]. A GA  
 515 is capable of exploring large multimodal search hypersurfaces  
 516 with unknown structures. It applies a set of specific selection  
 517 rules to evolve a population of individuals (possible solution  
 518 vectors) to a state that maximizes the “fitness” (or minimizes  
 519 the cost function) [24], [25]. It is known to have been success-  
 520 fully applied to complex numerical problems that cannot be  
 521 analytically solved. These include multimodal function op-  
 522 timization, pattern recognition, and parameter adaptation for  
 523 complex structures such as neural networks of different ar-  
 524 chitectures [23], [25]–[27]. A GA maintains a population of  
 525 individuals as a set of searching points and concurrently ex-  
 526 plores the search spaces along different directions. By applying  
 527 genetic operators such as crossover and mutation, a GA is  
 528 capable of moving an individual from one area on the search  
 529 hypersurface to another, possibly distant, area. This makes  
 530 it unlikely for the population to get stuck in local extrema.

Although a GA does not guarantee the global convergence, if  
 properly parameterized, it can greatly increase the probability  
 of finding the global optimum. Thus, in this paper, the GA is  
 chosen to perform the symbol dictionary generation.

The general GA framework—a set of special “genetic”  
 operators—evolves a population of individuals leading to adap-  
 tion by natural selection. Thus, optimization by the GA can  
 be expressed in the following form. First, a population of  
 individuals is selected at random from the entire solution space.  
 Hence, the population comprises a set of possible solutions to  
 the problem at hand. The fitness of each entity is assessed,  
 where the fitness represents the cost function being solved (or  
 its inverse). The population is then sorted based on the fitness to  
 ensure that the fitter individuals are more likely to be selected  
 for mating. The set of genetic operators such as crossover  
 (combining) and mutation (random alteration) is applied to the  
 selected individuals to produce new individuals or offspring,  
 which are added to the population. The fitness is reassessed,  
 and the least fit entities are removed from the pool. This process  
 of assessment, selection, offspring generation, and removal is  
 repeated until the desired performance has been achieved.

### C. Evolutionary Design Procedure

If the conventional competitive GA were applied to the  
 problem on hand, then an entire symbol dictionary would be  
 encoded into a single individual (member of the population).  
 These individuals would compete among themselves based on  
 the error rate they provided when loaded into the modem.  
 Then, after the evolution is finished, the “fittest” individual  
 would be the final dictionary for the modem. However, each  
 individual would have  $N_{\text{sym}} \times N_{\text{sam}}$  parameters, which poten-  
 tially could be large. Because of this high dimensionality, the  
 number of  $N_{\text{sym}} \times N_{\text{sam}}$  individuals should also be very large  
 to adequately cover the search space. To calculate the fitness  
 of each individual, each corresponding modem would need to  
 be simulated transmitting a statistically significant amount of  
 data through the voice codec. Although symbol generation is  
 an offline process, it could require a significant amount of time.

Hence, to reduce complexity of symbol generation, an alter-  
 native form of GA is used. In the cooperative GA [27], [28],  
 the entire population constitutes a single dictionary, with each  
 member of the population comprising a single symbol. The  
 result of the process is not a single optimal individual but is  
 instead a population of individuals coadapted to complement  
 one another, with the whole population representing the symbol  
 dictionary. To successfully develop a symbol dictionary in  
 this way, each individual symbol must evolve to occupy its  
 own “niche”—that is, it must not only perform well in its  
 own right (in this case, transfer through the voice codec with  
 minimal distortion) but must also be different enough from  
 the other symbols so that they can be reliably distinguished  
 by the MDP symbol decoder. How to develop this cooperative  
 behavior between members of a population is known as the  
 “niching problem” in GA literature [29]. In this paper, the  
 evolution of individuals that occupy their own niche is achieved  
 by choosing a GA fitness function that implicitly favors those  
 individuals that are different from the other symbols. This was

587 the approach to the cooperative GA taken by Whitehead and  
588 Choate [27]. Keeping this in mind, we are ready to outline  
589 the symbol-generation procedure. The process of generating  
590 symbols consists of the four steps described as follows.

- 591 1) Generate initial symbol set.
- 592 2) Select fittest symbols.
- 593 3) Produce new symbols, and update symbol set.
- 594 4) Iterate epochs: Repeat steps B and C until a sufficiently  
595 optimal symbol set is produced, or a maximum number  
596 of iterations is exceeded.

597 1) *Step A: Generate an Initial Symbol Set:* According to the  
598 chosen cooperative GA strategy, the entire population  $S$  of indi-  
599 viduals  $\mathbf{s}_i$ ,  $i = 1, 2, \dots, N_{\text{sym}}$  constitutes a single symbol set.  
600 Each individual  $\mathbf{s}_i$  consists of  $N_{\text{sam}}$  time samples. The symbols  
601 are generated in the frequency domain in such a way that they  
602 are real in the time domain. For the signal to be real in the time  
603 domain, it is required that the following conditions hold [15]:

$$\begin{cases} \text{Re}[\Phi] & \text{is even} \\ \text{Im}[\Phi] & \text{is odd} \end{cases} \quad (13)$$

604 where  $\Phi$  is the complex symbol spectrum. Hence, the  
605 symbol-generation procedure can be described as follows.

- 606 1) Randomly select a set of  $N_f$  complex numbers  $G_k$ ,  $k =$   
607  $1, 2, \dots, N_f$ , from  $\mathfrak{R}^2 \supset [-1, 1] \otimes [-1, 1]$  space. These  
608 numbers are used to produce the complex spectrum  $\Phi$  of  
609 the symbol and represent its active frequency load from  
610 dc (exclusive) to the Nyquist frequency. If  $N_f$  is less than  
611 the Fourier bin corresponding to the Nyquist frequency  
612  $N_N$ , then the unused  $N_N - N_f$  bins are zero padded.
- 613 2) Construct  $2N_f$  spectral components of  $\Phi$  using the num-  
614 bers  $G_k$  so that

$$\Phi_i = \begin{cases} 0, & \text{if } i = 0 \\ G_i, & \text{if } i = 1, \dots, N_f \\ 0, & \text{if } i = N_f + 1, \dots, N_N \\ G_{2N_N - i + 1}^*, & \text{if } i = N_N + 1, \dots, 2N_N \end{cases} \quad (14)$$

615 where the asterisk denotes a complex conjugate.

- 616 3) Apply the inverse discrete Fourier transform (DFT<sup>-1</sup>) to  
617  $\Phi$  to find the time-domain representation

$$\tilde{\mathbf{s}} = \text{DFT}^{-1}(\Phi). \quad (15)$$

- 618 4) Normalize the symbol power to produce the final time-  
619 domain symbol

$$\mathbf{s} = \frac{\tilde{\mathbf{s}}}{\|\tilde{\mathbf{s}}\|}. \quad (16)$$

620 These steps are repeated until all  $N_{\text{sym}}$  symbols are gener-  
621 ated. This process is similar to that in the *orthogonal frequency*  
622 *division multiplex* [30]. This way of generating a symbol guar-  
623 antees that it fits into the designated frequency band by design.  
624 2) *Step B: Select the Fittest Symbols:* Selection is a process  
625 in which fitter individuals are chosen to produce offspring for  
626 the next generation. The fitter symbols have a lower value of  
627 the cost function  $C(i)$ .

The modem is loaded with the dictionary of  $N_{\text{sym}}$  symbols 628  
that form the current population  $S$ . A pseudorandom datastream 629  
is then encoded into the symbols and sent through the vocoder. 630  
On the receiver side, the data are extracted by the MDP decoder, 631  
and the cost function  $C(i)$  for each  $i$ th symbol is calculated 632  
according to (12). The selection pressure is introduced for 633  
parents only, i.e., the  $N_{\text{off}}$  least fit parents are removed from the 634  
population to make room for the next generation of offspring. 635

“Ranking Selection” [31] is used to select pairs of individuals 636  
from the mating pool that will produce offspring for the next 637  
generation. It assigns selection probabilities  $P_{\text{sel}}(i)$  based on 638  
an individual’s rank  $R(i)$ , ignoring absolute fitness value. The 639  
individuals in the mating pool are sorted according to their 640  
fitness and then assigned a count  $R(i)$  that is simply their 641  
position in the sorted list. The best individual receives rank 1, 642  
the second best receives 2, and so on. The selection probability 643  
 $P_{\text{sel}}(i)$  is then specified as 644

$$P_{\text{sel}}(i) = C_s(1 - C_s)^{R(i)-1} \quad (17)$$

where  $C_s$  is a constant, such that  $0 < C_s < 1$ , which controls 645  
the slope of the  $P_{\text{sel}}$  distribution. The closer  $C_s$  is to 1, the 646  
more  $P_{\text{sel}}$  is weighted toward the fitter individuals,  $i = 1, 2,$   
647  $\dots, N_{\text{sym}}$ . Then, parents are selected by one roulette wheel 648  
rotation. For each  $N_{\text{off}}$  offspring, two parents are produced. 649

3) *Step C: Produce New Symbols and Update the Symbol* 650  
*Set:* The new symbol-generation process consists of two parts: 651  
1) *crossover* and 2) *mutation*. Crossover and mutation operate 652  
on the frequency-domain representation of the symbols to 653  
ensure that their spectra do not extend beyond the band limits. 654

- 1) *Crossover:* The new offspring is produced by a crossover 655  
process in which new individuals are generated by 656  
exchanging features of the selected parents. When the 657  
parents are represented by vectors of real numbers (real- 658  
coded GA), blend crossover BLX  $-\alpha$  [32] is known to 659  
provide a satisfactory combination of exploration and 660  
exploitation. Let us label two chosen parents  $\mathbf{G}^1$  and  $\mathbf{G}^2$ , 661  
where  $\mathbf{G}^i = \{G_k^i, k = 1, 2, \dots, N_f\}$ ,  $i = 1, 2$ . Then, the 662  
offspring  $\mathbf{G}'$  is generated by the BLX  $-\alpha$  crossover as 663  
follows: 664

$$\mathbf{G}' = \gamma \cdot \mathbf{G}^1 + (1 - \gamma) \cdot \mathbf{G}^2 \quad (18)$$

where  $\gamma$  is a uniformly distributed random variable on the 665  
interval  $[-\alpha, 1 + \alpha]$ . In this case,  $\alpha$  is chosen to be 0.5. 666

- 2) *Mutation:* The mutation process keeps the diversity of a 667  
population and promotes the search in the solution space 668  
that cannot be represented by the individuals of the cur- 669  
rent population. According to this process, a single ele- 670  
ment  $G_k^i$ ,  $k = 1, 2, \dots, N_f$  of the offspring  $\mathbf{G}'$  frequency 671  
representation, which is chosen at random, is replaced by 672  
a random complex variable from  $\mathfrak{R}^2 \supset [-1, 1] \otimes [-1, 1]$ . 673

Both of the genetic operators used in the offspring generation 674  
have nonunity probabilities of occurrence. The probability of 675  
crossover  $P_{\text{cross}}$  and the probability of mutation  $P_{\text{mut}}$  are 676  
usually empirically chosen [25], [33]–[35]. When the crossover 677



678 is not applied, the first parent  $\mathbf{G}^1$  is directly copied into the 679 offspring  $\mathbf{G}'$ . Then, the mutation operator is applied (or not) as 680 usual.

681 Generated offspring  $\mathbf{G}'$  is then used to construct the time- 682 domain symbols  $s_i$  using (14)–(16). After the new offsprings 683 have been generated, they replace the  $N_{\text{off}}$  least fit parents in 684 the population.

685 4) *Step D: Iterate Epochs:* Steps B and C are repeated until 686 one of the following conditions is met: A target error rate 687  $C_t$  is achieved or the maximum number of epochs  $N_{\text{epoch}}$  688 have passed. The number of epochs has to be chosen large 689 enough to allow GA convergence. Although replacing a large 690 fraction of the population at each epoch allows rapid evolution, 691 it stipulates a large residual error and can cause instability. To 692 address this issue, a variation of the “elitism” strategy is applied 693 [22]. The number of offsprings generated every epoch  $N_{\text{off}}$  was 694 reduced by one every  $N_{\text{reduct}}$  epochs, thereby minimizing the 695 residual error and providing “smoother” adaptation. For proper 696 operation, this requires the number of epochs  $N_{\text{epoch}}$  to be 697 equal to the initial number of offsprings multiplied by  $N_{\text{reduct}}$ , 698 so at the final stage of operation (last  $N_{\text{reduct}}$  generations), there 699 is one offspring being replaced every generation.

700 If there is no obvious target error rate for the application or 701 if it should simply be as low as possible, then the algorithm is 702 allowed to iterate for the full  $N_{\text{epoch}}$ . Alternatively, the symbol- 703 generation process can be stopped if there has not been any 704 improvement for a certain time period.

#### 705 D. Data Rate, Population Size, and Codebook Diversity

706 Let us denote the system data rate by  $R$ , which can be 707 calculated as follows:

$$R = f_s \cdot \eta \quad (19)$$

708 where  $f_s$  is the sampling frequency, and  $\eta$  is the coefficient 709 that determines the codebook properties. This coefficient will 710 be further referred to as the codebook diversity coefficient 711 (CDC), and it is calculated as a ratio between the number of 712 bits encoded into one symbol  $N_{\text{bit}}$  and the number of samples 713 per symbol  $N_{\text{sam}}$  given by

$$\eta = \frac{N_{\text{bit}}}{N_{\text{sam}}} = \frac{\log_2(N_{\text{sym}})}{N_{\text{sam}}} \quad (20)$$

714 It should be noted that some of the modem parameters 715 (e.g., sampling frequency  $f_s$  and designated bandwidth  $B$ ) are 716 specified by the GSM voice band and are fixed for all designs. 717 Hence, for the system under development, the data rate is 718 completely defined by the CDC.

719 As it can be seen in (19) and (20), the same CDC (and, 720 therefore, the same data rate) may be achieved by varying the 721 ( $N_{\text{bit}}$ ,  $N_{\text{sam}}$ ) pair. For example, to build a system with data rate 722 4000 b/s, the CDC must be equal to 1/2. This ratio may be 6/12 723 (6 b encoded into one 12-sample symbol), 7/14 (7 b encoded 724 into one 14-sample symbol), 8/16 (8 b encoded into one 16- 725 sample symbol), and so on, leading to  $64 \times 12$ ,  $128 \times 14$  and

TABLE I  
ALPHABET DESIGN PARAMETERS

$R, b/s$	$\eta$	$N_{\text{bit}}$	$N_{\text{sym}} \times N_{\text{sam}}$	$\Delta f, \text{Hz}$	$N_f$
2000	$\frac{1}{4}$	2	$4 \times 8$	1000	3
		3	$8 \times 12$	666.7	4
		4	$16 \times 16$	500	6
		5	$32 \times 20$	400	8
		6	$64 \times 24$	333.3	9
		7	$128 \times 28$	285.7	10
		8	$256 \times 32$	250	12
		9	$512 \times 36$	222.2	13
		4000	$\frac{1}{2}$	4	$16 \times 8$
5	$32 \times 10$			800	4
6	$64 \times 12$			666.7	4
7	$128 \times 14$			571.4	5
8	$256 \times 16$			500	6
9	$512 \times 18$			444.4	7

TABLE II  
COOPERATIVE GA PARAMETERS

$C_s$	$P_{\text{cross}}$	$P_{\text{mut}}$	$N_{\text{epoch}}$
0.075	0.9	0.1	26000

256  $\times$  16 codebooks, respectively. It will be shown in Section V 726 that the codebook (or the population) size affects both the sys- 727 tem performance and complexity. Thus, the goal is to identify 728 the codebook dimension (or a set of them) for each data rate, 729 which provides a tradeoff between the modem performance 730 and complexity. It should be noted that because the number of 731 bits per symbol  $N_{\text{bit}}$  (and, therefore, the population size  $N_{\text{sym}}$ ) 732 is the alphabet parameter responsible for the system data rate 733 and complexity, it is not a completely free GA parameter as 734 it is in the case of a conventional GA [25], [33], [34]. This 735 means that for a particular data rate  $R$ , the population size  $N_{\text{sym}}$  736 can only take values of 2, 4, 8, 16, and so on until it reaches 737 design constraints on the modem complexity. In addition,  $N_{\text{sym}}$  738 has to always be “balanced” by an appropriate symbol length 739  $N_{\text{sam}}$  to keep the target data rate constant. The number of 740 samples per symbol is, in turn, determined by the number of 741 active frequencies  $N_f$  used to construct the symbol. The symbol 742 active frequency load  $N_f$  is the important design parameter 743 as it defines the eigenstructure of the symbol dictionary and, 744 therefore, the dimensionality of the search space  $S$ . 745

Thus, the population (dictionary) size  $N_{\text{sym}}$  and the symbol 746 length  $N_{\text{sam}}$  need to be chosen according to practical concerns, 747 with data rate, error performance, and complexity all being 748 taken into consideration. 749

## V. SIMULATIONS

750

To assess the performance of our modem, we have gener- 751 ated a set of dictionaries corresponding to different data rates 752 using different sets of design parameters. The alphabet design 753 parameters are summarized in Table I, and the cooperative GA 754 parameters are represented in Table II. 755

For all alphabets, the sampling frequency  $f_s = 8000$  Hz and 756 the designated bandwidth  $B = [300, 3400]$  Hz were used. The 757 frequency spacing  $\Delta f$  and the number of active frequencies  $N_f$  758 were chosen in such a way that the symbol spectrum  $\Phi$  would 759 not extend beyond the designated frequency band  $B$  given by 760

$$\Phi \leq B. \quad (21)$$

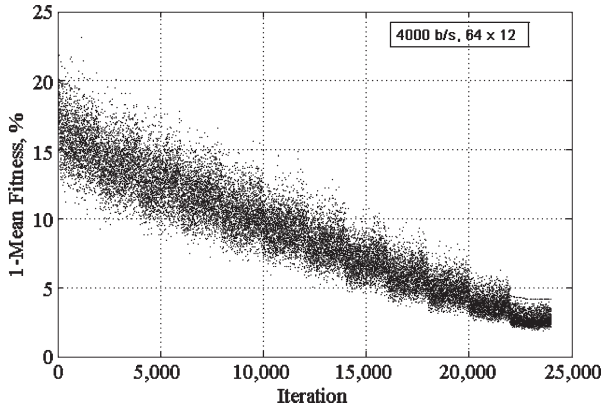


Fig. 6. Mean cost function convergence.

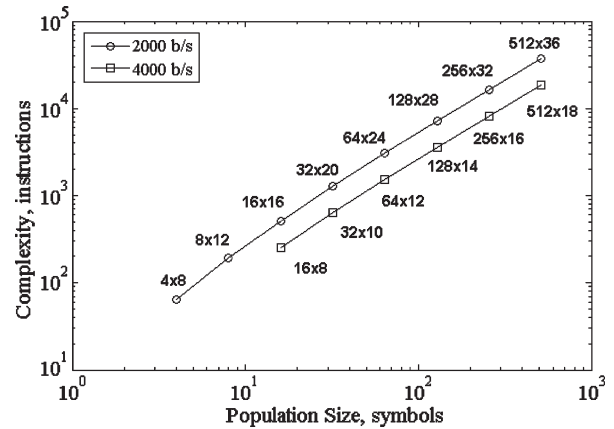


Fig. 8. Receiver complexity as a function of the population size.

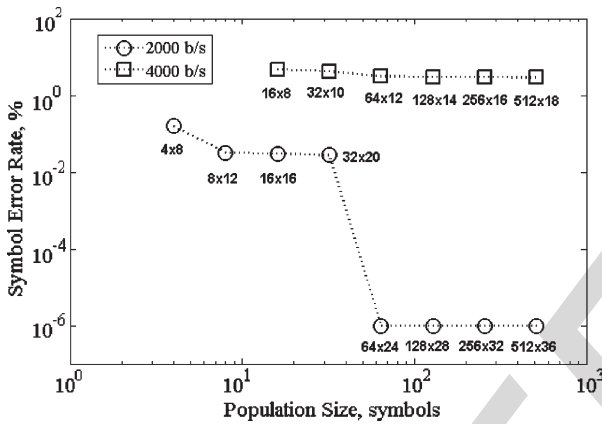


Fig. 7. SER as a function of the population size.

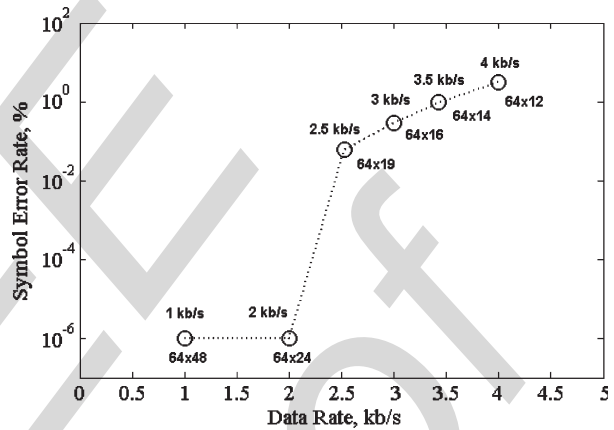


Fig. 9. SER as a function of the data rate.

761 All the symbol dictionaries were produced following the  
 762 steps A, B, C, and D described in the Section IV. There  
 763 were 26 000 epochs to generate each alphabet. The number of  
 764 offsprings was initially set to 12 and then decremented once in  
 765 2000 iterations.

766 Fig. 6 shows the convergence curve of the mean cost function  
 767 (which is one minus the mean fitness) generated for the data  
 768 rate equal to 4000 b/s and a codebook size of 64 symbols  
 769 by 12 samples. It took approximately from 22 000 to 25 000  
 770 iterations for the GA to converge to its error floor. It will be  
 771 seen that for the fixed population size, systems with lower data  
 772 rates have lower error floors. In addition, the cost function  
 773 has a variance decreasing with time and becomes more and  
 774 more “stair-like” as the elitism strategy reduces the number of  
 775 generated offsprings every 2000 iterations. It was noted that  
 776 the best fitness reached its maximum in a few iteration and  
 777 remained constant (or insignificantly changed) as the elitism  
 778 strategy preserved the best fit symbols.

779 Fig. 7 shows the error performance of the proposed modem  
 780 as a function of the population (codebook) size. The overall  
 781 modem error performance is determined by the CDC  $\eta$ . With  
 782 the CDC increased, the data rate  $R$  is also increased, but the  
 783 symbol error rate (SER) gets worse. Conversely, with the CDC  
 784 decreased, the data rate decreases, but the SER improves. This  
 785 result is intuitive and may be explained by the symbol diversity  
 786 concept—the longer the symbol (and, therefore, the richer its  
 787 frequency content) given the population (codebook) size, the

easier it is for the cooperative GA to maximize the Euclidian  
 788 distances between the symbols and, hence, to minimize the  
 789 SER. At the same time, the longer the symbol, given the  
 790 codebook size, the lower the data rate, as the same number  
 791 of bits is encoded into the longer symbols. Note that for the  
 792 codebook of the data rate of 4000 b/s, the error performance  
 793 slightly improves with the increase in the population size. The  
 794 SER reaches its floor of approximately 3% at a population  
 795 size of 64 symbols ( $64 \times 12$  alphabet), and a further increase  
 796 in the population size does not bring any significant SER  
 797 improvements. On the other hand, for the codebook of the data  
 798 rate of 2000 b/s, increasing the population size to 64 symbols  
 799 and above stipulates an SER better than  $10^{-6}$  (as  $10^6$  symbols  
 800 were used to evaluate the performance of each alphabet).  
 801

The complexity of the receiver as a function of the population  
 802 (codebook) size is depicted in Fig. 8. As the receiver complexity  
 803 grows as a power law of the population size, it is clear that the  
 804 codebook should be kept as compact as possible given the target  
 805 error rate.  
 806

Fig. 9 shows the error performance of the proposed data  
 807 communication system as a function of the data rate. The sys-  
 808 tem error performance gets worse with the data rate increased.  
 809 The reason for that, as was mentioned above, is in the reduction  
 810 of the search space dimensionality—the shorter the symbol,  
 811 given the fixed alphabet size, the harder it is for the GA to  
 812 minimize the overlap between the codewords.  
 813

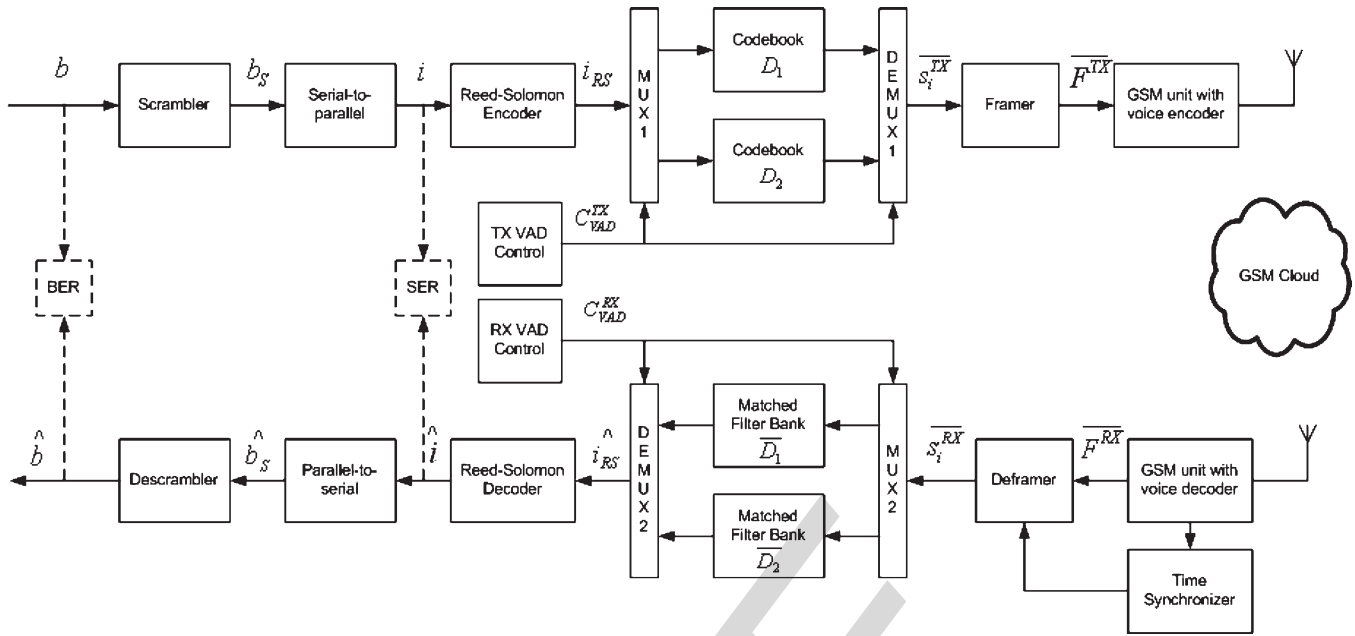


Fig. 10. Example system architecture that enables data transfer through the GSM-compressed voice channel.

814 In general, the system simulation results suggest the  
815 following.

- 816 1) The SER grows with the increased data rate.
- 817 2) The modem receiver complexity grows as a power law of  
818 the codebook size. Hence, there is a tradeoff between the  
819 modem receiver complexity and error performance.
- 820 3) An increase in the population (codebook) size brings  
821 some error performance improvement before reaching  
822 a certain limit where no further increase in it impacts  
823 the SER.
- 824 4) To design a modem that provides data rates greater than  
825 2000 b/s, some forward error correction should be in  
826 order. An appropriate FEC scheme for the system under  
827 development will be detailed in Section VI.

828 The simulations have also shown that the system perfor-  
829 mance was not sensitive to the cooperative GA parameters,  
830 so the authors followed the suggestions outlined in [25] and  
831 [33]–[35].

832 As mentioned above, the data modem described in this  
833 treatment uses the GSM voice channel as a backbone. The  
834 GSM physical layer has its own modulation, equalization, error  
835 detection, and FEC [7], [16] to alleviate the impact of multipath,  
836 noise, and interference, leaving the voice transcoding as the  
837 major source of errors. Nevertheless, it is clear that the overall  
838 performance of the modem under consideration is upper lim-  
839 ited by the GSM voice channel performance. A very detailed  
840 treatment on the GSM/GPRS performance may be found in [6].

## 841 VI. SYSTEM IMPLEMENTATION EXAMPLE

### 842 A. System Architecture

843 To use the developed modem in a real GSM environment, it is  
844 necessary to add some more components to the system. Fig. 10

illustrates an example system that enables data transfer over the  
845 GSM-compressed voice channel. 846

On the transmitter side, the input bitstream  $b$  is scrambled in  
847 the scrambler block to produce a randomized bitstream  $b_s$ . The  
848 scrambled bits  $b_s$  are fed into the serial-to-parallel block that  
849 converts it into  $N_{\text{bit}}$ -bit words  $i$ . The Reed–Solomon en- 850  
coder [36]–[38] buffers  $K_{\text{RS}} N_{\text{bit}}$ -bit payload words  $i$  and 851  
adds  $T_{\text{RS}}$  parity words to produce a Reed–Solomon codeword 852  
 $i_{\text{RS}}$  of length  $M_{\text{RS}} = K_{\text{RS}} + T_{\text{RS}} = 2^{N_{\text{bit}}} - 1$   $N_{\text{bit}}$ -bit words. 853  
This enables the correction of  $T_{\text{RS}}/2$  word errors in each 854  
Reed–Solomon codeword  $i_{\text{RS}}$ . Each  $N_{\text{bit}}$  sample of the 855  
Reed–Solomon codeword  $i_{\text{RS}}$  is used to address one of the 856  
codebooks  $\mathbf{D}_1$  or  $\mathbf{D}_2$ , depending on the state of the trans- 857  
mit multiplexer/demultiplexer pair MUX1/DEMUX1. The TX 858  
multiplexer/demultiplexer pair is controlled by the transmit 859  
TX VAD control block that progressively changes its output 860  
 $C_{\text{VAD}}^{\text{TX}}$  from “1” to “0” and *vice versa* every  $T_{\text{VAD}} = 80$  ms. 861  
Therefore, each Reed–Solomon-encoded  $N_{\text{bit}}$ -tuple is encoded 862  
into a symbol  $s_i^{\text{TX}}$ . These symbols are shifted into the Framing 863  
block where they are combined into packets  $F^{\text{TX}}$ , and a 864  
predefined preamble is added to each frame for synchronization 865  
purposes. The frames of the symbols are then passed into 866  
the GSM unit for over-the-air transmission. On the receiver 867  
side, the output of the GSM unit is the resynthesized symbol 868  
frame  $F^{\text{RX}}$ , which is the input to the frame synchronization 869  
unit that searches for the predefined preamble. As soon as the 870  
beginning of the frame is found, the deframer block is enabled, 871  
and the synchronization preamble is removed from the frame 872  
to produce data symbols  $s_i^{\text{RX}}$ . The matched-filter bank  $\mathbf{D}_1$  or 873  
 $\mathbf{D}_2$  is given a received symbol  $s_i^{\text{RX}}$ , depending on the state of 874  
the receive multiplexer/demultiplexer pair MUX2/DEMUX2, 875  
whose function is similar to the transmit pair. The matched- 876  
filter banks have the corresponding transfer functions  $\bar{\mathbf{y}}_1$  and  $\bar{\mathbf{y}}_2$  877  
and implement the MDP search to produce data estimate  $\hat{i}_{\text{RS}}$ . 878  
The mean symbols  $\bar{\mathbf{y}}_1$  and  $\bar{\mathbf{y}}_2$  were calculated offline during 879

880 the dictionary-generation process [see (7)]. The estimated data  
 881 words  $\hat{i}_{RS}$  are then used by the Reed–Solomon decoder, which  
 882 attempts to correct errors and outputs the estimates  $\hat{i}$  of the input  
 883 data words. The parallel-to-serial block converts the output  
 884 data words  $\hat{i}$  into the scrambled bits  $\hat{b}_s$ . The bitstream  $\hat{b}_s$  is  
 885 then passed to the descrambler block to produce the output  
 886 bitstream  $\hat{b}$ . To assess the modem performance, we use the  
 887 known input data to calculate the symbol and/or BER.

888 The Reed–Solomon source coding is the intuitive choice for  
 889 FEC because it operates on  $N_{bit}$ -bit words rather than bit-  
 890 streams. This complies with the fact that each symbol encodes  
 891  $N_{bit}$  bits of data; thus, errors occur in  $N_{bit}$ -bit blocks instead  
 892 of being evenly distributed. Thus, the ability of Reed–Solomon  
 893 codes to correct errors in  $N_{bit}$ -bit words makes it an efficient  
 894 FEC method for this application.

### 895 B. VAD

896 In addition to being robust to the voice codec, the designed  
 897 signal should not raise any alarms in the GSM system. The  
 898 GSM VAD is a technique designed to avoid transmission when  
 899 there is no speech. The VAD constantly monitors the signal  
 900 activity to determine if speech is present or if it is simply just  
 901 noise. If it concludes that there is no speech, it cancels transmis-  
 902 sion. This can cause problems for data transmission through the  
 903 GSM channel because it possesses noise-like features.

904 To ensure that the VAD indicates that there is voice present,  
 905 it is sufficient to dynamically vary the spectral envelope of the  
 906 signal over a time scale of approximately  $T_{vad} = 80$  ms, which  
 907 is the time interval that the VAD engine uses to gather statistics  
 908 about the speech signal. To implement this, the transmitter can  
 909 dynamically switch (once every  $T_{vad}$ ) between two symbol dic-  
 910 tionaries designed to have different spectral shapes. Of course,  
 911 this means that the same switching procedure is synchronously  
 912 performed on the receiver side. Dictionaries with different  
 913 spectral shapes can be generated by varying the active Fourier  
 914 bins [see (14)]. The response of the VAD was from the direct  
 915 observation of the VAD flag in the software simulation of the  
 916 GSM vocoder system.

### 917 C. Prototype System Test

918 The system described above was implemented and suc-  
 919 cessfully tested over the air. The prototype mobile unit was  
 920 developed as a custom-designed single-board computer with a  
 921 host processor based on the ARM920T embedded core and a  
 922 Sony Ericsson GSM module. The modem used the following  
 923 parameters: dictionary size  $N_{sym} = 64$  symbols, symbol length  
 924  $N_{sam} = 12$  samples, number of active carriers  $N_f = 3$ , and raw  
 925 data rate  $R = 4000$  b/s, with the rest of the modem parameters  
 926 the same as in Section V. The Reed–Solomon code parameters  
 927 were chosen to be  $M_{RS} = 63$ ,  $K_{RS} = 45$ , and  $T_{RS} = 18$ . This  
 928 means that the FEC overhead was 30% and correcting capabili-  
 929 ties were 15%. For a 40-min call of continuous data transmission  
 930 (approximately 6720 kb of random data), it produced 26 erro-  
 931 neous bits, giving a BER of  $4 \times 10^{-6}$ . The data transmission  
 932 did not cause any alarm (such as VAD) to be triggered, so as far  
 933 as the GSM system was aware, it was a normal voice call.

As already mentioned, once generated, the symbol set is 934  
 loaded into the modem and needs no more changes. Thus, 935  
 the dictionary generation can be performed offline, and the 936  
 complexity of this process is not of a high priority. Therefore, 937  
 the symbols can be generated using any high-level modeling 938  
 languages such as Matlab to avoid unnecessary development 939  
 effort. 940

### D. Performance and Complexity Analysis 941

Although the system development is performed offline, to 942  
 be used in a real communication system such as a GSM 943  
 data modem, the complexity of the receiver must allow real- 944  
 time embedded system implementation. It should be noted that 945  
 the data-to-symbol-encoding process is merely a table lookup, 946  
 whereas the symbol-to-data decoding involves MDP symbol 947  
 detection. Thus, the complexity of the encoding process is 948  
 negligible compared to the decoding. Hence, the detection 949  
 algorithm complexity and code efficiency in terms of millions 950  
 of instructions per second is imperative. 951

Below is the performance and complexity comparisons 952  
 between the systems described in [17] and in this paper. 953  
 According to [17], a real-time prototype was implemented 954  
 to demonstrate one-way encrypted communications over the 955  
 GSM-compressed voice channel using a single transmitter/ 956  
 receiver pair. The transmitter/receiver pair required two 2-GHz 957  
 Intel processor-based Windows computers, each having 2 GB 958  
 of random access memory and a Creative Sound Blaster Audigy 959  
 soundcard. Both computers were interfaced to GSM Nokia 960  
 handsets—one for the transmitter and one for the receiver. A 961  
 raw (uncoded) data rate of 3 kb/s has been reported with a 2.9% 962  
 BER. Adding error correcting codes (rate 1/2 convolutional 963  
 codes) yielded a throughput of 1.2 kb/s with a 0.03% BER. 964

On the other hand, the GSM data modem described in this 965  
 treatment has been implemented as a portable device based 966  
 on one 50-MHz ARM920T embedded processor and one Sony 967  
 Ericsson GSM unit. This handheld GSM modem provided full- 968  
 duplex communications through the compressed GSM voice 969  
 channel with an uncoded data rate of 4 kb/s and an SER of less 970  
 than 3%. The Reed–Solomon coded data rate was 2.8 kb/s with 971  
 a BER of better than  $4 \cdot 10^{-6}$ . The software was run on an ARM 972  
 processor that included an operating system, a proprietary 973  
 medium access control/link layer, drivers, and the application 974  
 program. Thus, the modem presented here produced a higher 975  
 data rate, less errors, and a significantly lower complexity than 976  
 the system described in [17] for data transfer through the GSM 977  
 voice channel. 978

It should be noted that there is a tradeoff between the data 979  
 rate, error rate, and complexity. For example, to improve the 980  
 error rate, the symbol length  $N_{sam}$  should be increased (see 981  
 Fig. 9). However, this would reduce the data rate for a given 982  
 dictionary size  $N_{sym}$ . In response, increasing the dictionary size 983  
 would increase the search time of the MDP decoder, leading to 984  
 a higher computational burden. 985

## VII. DISCUSSION AND CONCLUSION 986

In this paper, we have described a new method to trans- 987  
 fer data through the compressed GSM voice channel, which 988

989 involves the evolutionary synthesis of the signal. The chosen  
 990 application to demonstrate this design concept was to commu-  
 991 nicate data through the GSM voice channel. Simulations have  
 992 shown that it was possible to achieve data communications  
 993 through this highly nonlinear system. The next logical step,  
 994 following the simulations, was to implement a real modem for  
 995 over-the-air communications. A portable device implementing  
 996 the modem presented here was developed and successfully  
 997 tested in Australia on the three major GSM networks, yielding  
 998 a raw data rate of 4 kb/s.

999 A GSM modem of the type described here would be  
 1000 useful in applications such as telemetry, secure communica-  
 1001 tions, wireless automatic teller machines, and faxes—virtually  
 1002 anywhere—where the regular transmission of low-rate data  
 1003 bursts is required. A great advantage of this type of system is  
 1004 that a data service can be deployed where there is no cabling or  
 1005 wireless data channel. Using only a voice channel leads to low  
 1006 setup and maintenance costs and independence from the carrier.  
 1007 For the carrier, the data transmission is just a normal voice  
 1008 call. This may be seen as a “virtual network,” or a “network  
 1009 within network,” providing new services without the need to  
 1010 upgrade the carrier network. Even when there is a dedicated  
 1011 data channel, e.g., GPRS, already in place, a system to transfer  
 1012 data through the voice channel would allow greater options to  
 1013 balance the system load or create a higher priority datastream  
 1014 for lower data rate but “mission-critical” applications. The  
 1015 GSM voice channel was chosen for its ubiquity, low cost,  
 1016 and great coverage, but the type of modem developed here  
 1017 potentially could be used to communicate data through any  
 1018 compressed voice channel.

1019 Although in this paper we have confined our investigations  
 1020 to the GSM EFRV, it is envisaged that this approach should  
 1021 be applicable to other voice codecs. Such a modem would be  
 1022 designed by simply replacing the EFRV by the other codec in  
 1023 the evolutionary optimization of symbols to produce a set of  
 1024 symbols optimized to be robust through transmission through  
 1025 the new codec. The optimization procedure described here will  
 1026 find such a symbol set if the cost function for the new codec is  
 1027 not significantly more complex than that produced by the EFRV.  
 1028 Whereas this conjecture is unproven, we believe it to hold  
 1029 due to the similarity in the mathematical form of the speech  
 1030 models in commonly used codecs. Initial tests with other voice  
 1031 codecs, such as the GSM half-rate vocoder [7], [12], have been  
 1032 successful, but this work is still ongoing.

1033 The central innovation guiding this work is the evolutionary  
 1034 adaptation to the compressed voice channel, which is impossi-  
 1035 ble to invert due to its nonlinear lossy nature. This represents  
 1036 a new framework for the communication system design. The  
 1037 signal set is adapted to the voice codec by natural selection.  
 1038 The general concept of “adaptation to fit the channel” could  
 1039 potentially be applied to any receiver structure and signal type.

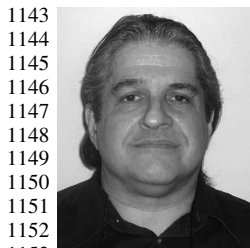
#### 1040 REFERENCES

1041 [1] 3GPP TS 43.064, Overall Description of the GPRS Radio Interface;  
 1042 Stage 2.  
 1043 [2] M. F. Madkour, “Effect of high GSM voice traffic on GPRS data net-  
 1044 work and the proposed solutions,” in *Proc. 46th IEEE Int. MWSCAS*,  
 1045 Dec. 27–30, 2003, vol. 3, pp. 1259–1262.

[3] S. Ni and S. Haggman, “GPRS performance estimation in GSM circuit 1046  
 switched services and GPRS shared resource systems,” in *Proc. IEEE 1047  
 WCNC*, Sep. 1999, pp. 1417–1421. 1048  
 [4] I. Goetz, “Keeping up with GPRS,” *Commun. Eng.*, vol. 1, no. 2, p. 46, 1049  
 Apr./May 2003. 1050  
 [5] T. Alanko, M. Kojo, H. Laamanen, M. Liljeberg, M. Moilanen, and 1051  
 K. Raatikainen, “Measured performance of data transmission over 1052  
 cellular networks,” Dept. Comput. Sci., Univ. Helsinki, Helsinki, Finland, 1053  
 Rep. C-1994-53, 1994. 1054  
 [6] T. Halonen, J. Romero, and J. Melero, *GSM, GPRS and EDGE Perfor-* 1055  
*mance*, 2nd ed. Chichester, U.K.: Wiley, 2003. 1056  
 [7] S. Redl, M. Weber, and M. W. Oliphant, *GSM and Personal Communica-* 1057  
*tions Handbook*. Norwood, MA: Artech House, 1998. 1058  
 [8] H.-H. Liu and J. L. C. Wu, “Delay analysis of integrated voice and data 1059  
 service for GPRS,” *IEEE Commun. Lett.*, vol. 6, no. 8, pp. 319–321, 1060  
 Aug. 2002. 1061  
 [9] S. Hamiti, M. Hakaste, M. Moision, N. Nefedov, E. Nikula, and 1062  
 H. Vilpponen, “EDGE circuit switched data—An enhancement of GSM 1063  
 data services,” in *Proc. IEEE WCNC*, 1999, pp. 1437–1441. 1064  
 [10] R. Mullner, C. F. Ball, K. Ivanov, F. Treml, and G. Spring, “Quality of 1065  
 service in GPRS/EDGE mobile radio networks,” in *Proc. IEEE 59th Veh. 1066  
 Technol. Conf.*, 2004, vol. 5, pp. 2507–2511. 1067  
 [11] *Digital Cellular Telecommunications Systems (Phase 2+); Enhanced Full 1068  
 Rate (EFR) Speech Transcoding; (GSM 06.60 Version 8.0.1. Release 1069  
 1999)*, 2000. Available: ETSI EN 300 726. 1070  
 [12] R. Meston, *Sorting Through GSM Codecs: A Tutorial*. Irvine, CA: Racal 1071  
 Instruments, Jul. 2003. [Online]. Available: <http://www.commsdesign.com/showArticle.jhtml?articleID=16501605> 1072  
 [13] D. G. Manolakis, V. K. Ingle, and S. M. Kogon, *Statistical and Adaptive 1073  
 Signal Processing*. New York: McGraw-Hill, 2000. 1074  
 [14] S. Haykin, *Communication Systems*, 4th ed. New York: Wiley, 2001. 1075  
 [15] C. L. Phillips and J. M. Parr, *Signals, Systems and Transforms*. Upper 1076  
 Saddle River, NJ: Prentice-Hall, 1995. 1077  
 [16] *Digital Cellular Telecommunications Systems (Phase 2+); Physical 1078  
 Layer on the Radio Path; General Description; (GSM 05.01 Version 7.1.0. 1080  
 Release 1998)*, 1998. Available: ETSI TS 100 573. 1081  
 [17] N. N. Katugampala, K. T. Al-Naimi, S. Villette, and A. M. Kondoz, “Real 1082  
 time data transmission over GSM voice channel for secure voice and 1083  
 data applications,” in *Proc. 2nd IEE Secure Mobile Commun. Forum: 1084  
 Exploring Tech. Challenges Secure GSM WLAN (Ref. No. 2004/10660)*, 1085  
 Sep. 23, 2004, pp. 7/1–7/4. 1086  
 [18] N. N. Katugampala, S. Villette, and A. M. Kondoz, “Secure voice 1087  
 over GSM and other low bit rate systems,” in *Proc. IEE Secure GSM 1088  
 Beyond: End to End Security Mobile Commun.*, London, U.K., Feb. 2003, 1089  
 pp. 3/1–3/4. 1090  
 [19] M. R. Schroeder and B. S. Atal, “Code excited linear prediction (CELP): 1091  
 High quality speech at very low bit rates,” in *Proc. ICASSP*, 1985, 1092  
 pp. 937–940. 1093  
 [20] J. Proakis, *Digital Communications*, 4th ed. New York: McGraw-Hill, 1094  
 2001. 1095  
 [21] *Digital Cellular Telecommunications Systems (Phase 2+); ANSI-C Code 1096  
 for the GSM Enhanced Full Rate (EFR) Speech Codec; (GSM 06.53 1097  
 Version 8.0.1. Release 1999)*, 2000. Available: ETSI EN 300 724. 1098  
 [22] R. L. Haupt and S. E. Haupt, *Practical Genetic Algorithms*. Hoboken, 1099  
 NJ: Wiley, 2004. 1100  
 [23] B. Bhanu, Y. Lin, and K. Krawiec, *Evolutionary Synthesis of Pattern 1101  
 Recognition Systems*. New York: Springer-Verlag, 2005. 1102  
 [24] J. Holland, *Adaptation in Natural and Artificial Systems*, 2nd ed. 1103  
 Cambridge, MA: MIT Press, 1992. 1104  
 [25] D. E. Goldberg, *Genetic Algorithms in Search, Optimization and Machine 1105  
 Learning*. Boston, MA: Addison-Wesley, 1989. 1106  
 [26] J. D. Schaffer, L. D. Whitley, and L. J. Eshelman, “Combinations of 1107  
 genetic algorithms and neural networks: A survey of the state of the art,” 1108  
 in *Proc. Int. Workshop Combination Genetic Algorithms Neural Netw.*, 1109  
 L. D. Whitley and J. D. Schaffer, Eds., 1992, pp. 1–37. 1110  
 [27] B. A. Whitehead and T. D. Choate, “Cooperative-competitive genetic 1111  
 evolution of radial basis function centers and widths for time series 1112  
 prediction,” *IEEE Trans. Neural Netw.*, vol. 7, no. 4, pp. 869–880, 1113  
 Jul. 1996. 1114  
 [28] M. A. Potter and K. A. De Jong, “A cooperative coevolutionary approach 1115  
 to function optimization,” in *Proc. 3rd PPSN*, 1994, pp. 249–257. 1116  
 [29] K. Deb and D. E. Goldberg, “An investigation of niche and species for- 1117  
 mation in genetic function optimization,” in *Proc. 3rd Int. Conf. Genetic 1118  
 Algorithms*, 1989, pp. 42–50. 1119  
 [30] L. Hanzo, M. Münster, B. J. Choi, and T. Keller, “OFDM and MC-CDMA 1120  
 for broadband multi-user communications,” in *WLANs and Broadcasting*. 1121  
 Chichester, U.K.: Wiley, 2003. 1122



- 1123 [31] F. Hoffmeister and T. Bäck, "Extended selection mechanism in genetic  
1124 algorithms," in *Proc. 4th Int. Conf. Genetic Algorithms*, 1991, pp. 92–99.
- 1125 [32] L. J. Eshelman and J. D. Schaffer, "Real-coded genetic algo-  
1126 rithms and interval-schemata," in *Foundation of Genetic Algorithms*,  
1127 vol. 2, L. D. Whitley, Ed. San Mateo, CA: Morgan Kaufmann, 1993,  
1128 pp. 187–202.
- 1129 [33] J. J. Grefenstette, "Optimization of control parameters for genetic  
1130 algorithms," *IEEE Trans. Syst., Man, Cybern.*, vol. SMC-16, no. 1,  
1131 pp. 122–128, Jan./Feb. 1986.
- 1132 [34] R. L. Haupt, "Optimum population size and mutation rate for a simple real  
1133 genetic algorithm that optimizes array factors," in *Proc. IEEE Antennas  
1134 Propag. Soc. Int. Symp.*, Jul. 16–21, 2000, vol. 2, pp. 1034–1037.
- 1135 [35] K. A. De Jong, "Analysis of the behavior of a class of genetic adaptive  
1136 systems," Ph.D. dissertation, Univ. Michigan, Ann Arbor, MI, 1975.
- 1137 [36] S. Lin and D. J. Costello, Jr., *Error Control Coding: Fundamentals and  
1138 Applications*. Englewood Cliffs, NJ: Prentice-Hall, 1983.
- 1139 [37] T. K. Moon, *Error Correction Codes: Mathematical Methods and  
1140 Algorithms*. Hoboken, NJ: Wiley, 2005.
- 1141 [38] S. B. Wicker, *Error Control Systems for Digital Communications and  
1142 Storage*. Upper Saddle River, NJ: Prentice-Hall, 1995.



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## AUTHOR QUERIES

AUTHOR PLEASE ANSWER ALL QUERIES

AQ1 = 3166 was used as the postal [zip codes are US only] code. Please check if correct.

AQ2 = The paragraph starting with “It converts input data...” was connected to the previous paragraph for continuity. Please check if correct.

AQ3 = “problematic” was changed to “difficult.” Please check if correct.

AQ4 = “or” was inserted for clarity.

AQ5 = “or simply noise” was changed to “or if it is simply just noise” for clarity. Please check if correct.

AQ6 = “by” was changed to “from the” for clarity. Please check if correct.

AQ7 = “MIPS” was expanded as “million instructions per second.” Please check if correct.

AQ8 = Please specify the type of degree earned.

AQ9 = “Kharkov University” was changed to “Kharkov State University.” Please check if correct.

Notes: 1) “European Telecommunications Standards Institute” was deleted in Refs. [11], [16] and [21]. Please check.

2) “Los Alamos: IEEE Comput. Society Press” was deleted in Ref. [26]. Please check.

3) “San Francisco, CA: Morgan Kaufmann” was deleted in Ref. [28]. Please check.

4) “San Mateo, CA: Morgan Kaufmann” was deleted in Ref. [31]. Please check.

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